

The Fast Floating-Point Library

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0 Revision History

Date	Revision(s)
12/13/2006	Finished first final copy of report
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1 Introduction

The goal of our project was to create an efficient (low-power), robust, versatile, and autonomous walking quadruped (four-legged) robot. A walking robot that mimics the human gait has important applications in the field of medicine. For example, if a walking robot can be designed, a “wheelchair” that has legs instead of wheels can be designed. Such a device would enable the handicapped to travel up and down stairs, eliminating the need for wheelchair ramps. Someday, we might be able to replace prosthetics with powered robotic legs for people who have lost the ability to walk.

The most efficient robots, also known as passive-dynamic robots, walk by mimicking the human gait, and use gravity to travel down a slope. However, they cannot walk on flat ground, and will topple even if the surface beneath them is only slightly uneven, making them neither versatile nor robust. Our robot, the Cornell Ranger, uses a microcontroller to monitor and guide its motions. It has an outer pair and an inner pair of legs, and each leg has a movable ankle, whose motion is controlled by foot sensors. The robot walks by lowering the ankles on its front pair of legs when its front feet are near the ground, pushing off the ground with the heels of its front feet, and using its own momentum to swing the back pair of legs forward. Whenever the back pair of legs is swinging forward, the ankles are raised to prevent the feet from dragging on the ground.

The microcontroller¹ monitors each part of the robot’s walk, and provides extra power to the ankles during push-off of the foot. This enables the robot to walk on flat ground (and even uphill on shallow slopes), and increases the robot’s stability as well (even though the feet on our robot were less than an inch wide, our robot was able to walk on an indoor track, which does not have a smooth surface). But since the microcontroller needs to be powered, our robot uses more power than gravity-based passive-dynamic robots.

Our microcontroller is designed to execute a list-of commands once every millisecond. These commands include determining hip and feet angles, and position of the feet relative to the ground, among other things. Therefore, our Digital Signal Processing (DSP) unit², which handles all of the calculations, must be able to quickly and accurately handle large ranges of numbers with relatively high precision. In addition, basic arithmetic operations, such as addition, subtraction, multiplication, division, and comparisons, must be done quickly.

This is where the FFloat (fast floating-point) numbers come in. This report will describe what FFloat numbers are, why we used them in the software of our robot, and how we developed the FFloat library of functions. A brief description of each of the functions in the FFloat library will then be given along with runtime (cycle count) data for all of the FFloat functions. Appendix A presents an overview of two’s complement and Appendix B contains the source code for the FFloat functions the author developed. Hopefully, the functions we wrote for the FFloat library, as well as the methods we used to develop the library, will be useful in future research and development where efficient and accurate data processing is critical.

¹ The MC56F8347, made by Freescale Semiconductor, is a 16-bit hybrid controller with an integrated 16-bit DSP chip (the DSP56800E) [1].

² The DSP56800E, also made by Freescale Semiconductor. It is a low-power, fast 16-bit DSP [2].

2 Why Use FFloat?

This section will attempt to motivate the decision to use FFloat numbers as the standard numerical type for performing calculations in the Cornell Ranger. The FFloat numerical type is a very non-intuitive, and non-standard way to represent numbers, but as we will see shortly, it was our best option.

There are two other numerical types that could have been used in place of FFloat: IEEE floating-point and fixed-point. IEEE floating-point is implemented into the C programming language as the float type. Fixed-point type uses scaled, or normalized, integers to represent fractional values.

The most important factor in deciding which numerical type to use was speed. Our microcontroller is designed to run its code indefinitely through a 1-millisecond loop, and our microprocessor only allows for 60000 cycles per loop. Therefore, our functions needed to be fast, requiring as few cycles as possible. With this in mind, we decided that IEEE-float was too slow for use in our microprocessor. For example, an arithmetic operation as simple as addition takes 250 cycles, which means that with IEEE-float, each loop will only be, at best, capable of performing 240 additions. IEEE-float also has many features that we did not need, such as error handling for NaN (not a number) and representation for positive and negative infinity. These cases would have to be handled in all IEEE floating-point functions, greatly increasing the number of cycles needed to run the functions.

Fixed-point notation, on the other hand, is fast because it uses integers instead of floating-point values. The problem with fixed-point, however, is that many digits are required in order to accurately represent numbers that require several decimal places. If too few digits are used, the precision of the resulting number will be too poor to use, and if too many digits are used, the number could overflow, giving clipped data, which would give a completely incorrect result.

In addition, fixed-point numbers must be scaled properly in order for fixed-point operations to work properly. Trying to figure out the scaling for every parameter during software development is time-consuming and prone to error. With floating-point numbers, the exponent automatically takes care of the scaling. This eliminates the need to manually scale floating-point numbers, reducing development time, as well as the time needed to fix bugs caused by incorrectly scaling numbers.

In short, FFloat numbers surpass IEEE floating-point in speed and fixed-point in precision and ease-of-use. Part of the reason that IEEE floating-point was so slow was that our DSP chip did not have a floating-point co-processor. For our next robot, we will be using a DSP chip with a floating-point co-processor, which will probably reduce code development time significantly.

3 An Overview of FFloat Numbers

3.1 Format for FFloat Numbers

FFloat numbers are 32-bit³ binary numbers. They are represented by a mantissa (a fractional value) multiplied by a base number raised to an exponent (an integral value).

The mantissa is a signed two's complement⁴ 16-bit binary number, and is represented by the rightmost 16 bits of the FFloat number. It has a range between -2^{15} (-32768 , $0x8000$)⁵ and $2^{15}-1$ (32767 , $0x7FFF$), but is interpreted as a fractional value between -1 (inclusive) and 1 (exclusive). To get the real fractional value, divide the FFloat mantissa value by 2^{15} .

The exponent is also a signed two's complement 16-bit binary number, and is represented by the leftmost 16 bits of the FFloat number. Though we have 16 bits to work with, we will only be using the bottom 8 bits to represent the exponent value, which means that the range of the exponent is between -2^7 (-128 , $0xFF80$) and 2^7-1 (127 , $0x007F$). The top 8 bits of the exponent are sign bits: all ones for negative values, and all zeros for nonnegative values.

To get the real floating-point numerical value, we take the real fractional value of the FFloat mantissa and multiply it by 2 raised to the exponent of the FFloat number:

$$\text{numerical value} = (\text{FFloat mantissa}/2^{15}) \times 2^{(\text{FFloat exponent})}.$$

Even though we are only using 8 bits to represent the exponent, we can represent numbers between 2^{-128} (2.93×10^{-39}) and 2^{127} (1.70×10^{38}), which is more than sufficient for our calculations.

For convenience, we will represent FFloat numbers in hexadecimal rather than in binary, so that only 8 digits, instead of 32, are needed (a hexadecimal number can be represented by a 4-bit binary number).

3.2 Handling Exceptional Values

For FFloat numbers, there are three types of values that must be handled in a special manner: zero, overflow values, and underflow values.

Zero: We have decided to set zero equal to $0xFF800000$. The mantissa is zero, and the exponent is set to its most negative value (-2^7). It was determined that if zero is defined this way, our FFloat addition and subtraction functions could be written without special exception handling for adding or subtracting zero, thereby saving processing time.

Overflow: Occurs if the magnitude of an FFloat number is larger than $0x007F7FFF$ (for positive values) or $0x007F8000$ (for negative values). To check for overflow, the exponent of the FFloat number is compared to the value $0x007F$ (2^7-1)⁶. If the FFloat number is determined to be too

³ A bit is a 1 or 0.

⁴ See Appendix A (Section 6) for a more in-depth discussion on two's complement.

⁵ By convention, hexadecimal numbers are preceded by the characters 0x.

⁶ We used the built-in assembly instruction `cmp.w`, which compares two 16-bit words.

large in magnitude, the sign of the overflow (positive or negative) is then determined by comparing the FFloat number's mantissa value to the mantissa values 0x7FFF and 0x8000⁷. The overflow number is then set to the maximum positive or negative number as appropriate.

Underflow: Occurs if the magnitude of an FFloat number is smaller than 0xFF804000 (for positive values) or 0xFF80BFFF (for negative values). To check for underflow, the exponent of the FFloat number is compared to the value 0xFF80 (-2^7). If the FFloat number is determined to be too small in magnitude, the sign of the overflow (positive or negative) is then determined by comparing the FFloat number's mantissa value to the mantissa values 0x4000 and 0xBFFF. The underflow number is then set to the minimum positive or negative number as appropriate.

Overflow range: less than 0x007F8000 (-2^{127}) or greater than 0x007F7FFF ($.99997 \times 2^{127}$)

Underflow range: between 0xFF80BFFF ($-.50003 \times 2^{-128}$) and 0xFF804000 ($.5 \times 2^{-128}$)

In our FFloat library functions, the Zero case is handled before the Underflow case so that the underflow check does not throw out an input of zero.

3.3 Using FFloat Numbers

3.3.1 Declaring and Initializing FFloat numbers in C

Since the `ffloat`⁸ type is not defined in C, any program that uses `ffloat` numbers must include the following type definition statement:

```
typedef long unsigned int ffloat;
```

There are two ways to initialize an FFloat number. The first is to initialize it directly, by setting the variable equal to a hexadecimal number. For example, to initialize the `ffloat` variable `ffnumA` to zero, use the following statement:

```
ffloat ffnumA = 0xFF800000;
```

The second way is to use one of the two integer-to-FFloat conversion functions, both of which are part of the FFloat library. To initialize `ffnumA` to zero using the functions, use the following statement:

```
ffloat ffnumA = S16int2FFloat(0);
```

`S16int2FFloat` and `S32int2FFloat` are the two integer-to-FFloat conversion functions, and `IEEE2FFloat` is the standard float-to-FFloat conversion function. They will be discussed in greater detail in Section 4, along with the other FFloat library functions.

⁷ We used the built-in assembly instruction `tst.w`, which compares a 16-bit word to zero.

⁸ `ffloat` is the type definition for FFloat that was used in our C code.

3.3.2 Performing Operations on FFloat Numbers

Since FFloat numbers are not standard numerical types in C, there are no operators in C defined for FFloat numbers. Therefore, you must replace the arithmetic operators (+, -, ×, ÷) and the comparison operators (>, <, ≥, ≤, =) with the appropriate function in the FFloat library.

Use of the trigonometric, conversion, and absolute value functions is similar to that in IEEE floating-point.

4 The FFloat Library

4.1 Development of the FFloat Library

After deciding to use FFloat numbers, we had to decide which functions we needed for the FFloat library. A disadvantage of FFloat numbers is that they are not a standard type in C. Therefore, we had to write functions for the basic arithmetic operators (+, -, ×, ÷) and comparison operators (>, <, ≥, ≤, =), and use these functions in place of the operators. The trigonometric functions were developed because we needed a way to determine hip and foot angles in order to detect, for example, when the foot was about to touch the ground. Most of the other functions, such as taking the negative of a number and finding the absolute value of a number, were developed for use in the trigonometric functions and in the main C code.

In developing the FFloat library, we used CodeWarrior, a product of Metrowerks. We chose CodeWarrior for two main reasons: 1) it allowed us to write assembly code and C code in the same file (functions written in assembly code always start with the keyword `asm`), and 2) it supports the DSP56800, the DSP chip used in our microcontroller. As an added feature, CodeWarrior has a built-in DSP56800 simulator, which allowed us to measure the number of cycles and instructions required by the DSP56800 to execute a specific block of code (we designated this block of code using breakpoints).

The `S16int2FFloat`, `S32int2FFloat`, and `IEEE2FFloat` conversion functions (see Section 4.2) were the first to be developed. These functions were verified by calculating the expected FFloat value by hand, then printing out the output of the function to see if it matched our prediction. Once these three functions were written, checking the output of all the other FFloat functions was easy. As an example, here is how `FFadd` would have been verified:

1. Define `ffloatA = S16int2FFloat(a)` and `ffloatB = S16int2FFloat(b)`, where `a` and `b` are 16-bit integers (short int). `S32int2FFloat` or `IEEE2FFloat` could also be used, based on the range of numbers that needed to be added.
2. Run `FFadd(ffloatA, ffloatB)` and print out the output.
3. Print out the value `S16int2FFloat(a+b)` and see if it matched the output given by `FFadd`.
4. Test all possible branches of `FFadd`, including exception cases such as overflow.

To reduce the cycle count, we wrote all of our functions in assembly (the trigonometric functions were written in C, however, because they were too complex to program in assembly).

Since we spent less than a month working on the FFloat library, we did not have time to optimize the assembly code that we wrote. However, our cycle count data will be useful in determining

which functions need to be optimized, and optimization of our functions in the future, when we have more time, is something that should be considered.

4.2 *FFloat Library Functions*

This section lists all the functions in the FFloat library by their function headers, and gives a brief description of what the functions return.

Standard arithmetic operations

asm ffloat FFadd(register ffloat fnum1, register ffloat fnum2) – returns $\text{fnum1} + \text{fnum2}$.

asm ffloat FFsub(register ffloat fnum1, register ffloat fnum2) – returns $\text{fnum1} - \text{fnum2}$.

asm ffloat FFlmult(register ffloat fnum1, register ffloat fnum2) – returns $\text{fnum1} \times \text{fnum2}$.

asm ffloat FFdiv(register ffloat fnum1, register ffloat fnum2) – returns $\text{fnum1} / \text{fnum2}$.

Trigonometric functions

ffloat FFsin(ffloat xin) – returns the sine of xin.

ffloat FFlcos(ffloat xin) – returns the cosine of xin.

ffloat FFatan(ffloat xin) – returns the arctangent of xin.

Comparison functions

asm bool⁹ FFlgt(register ffloat fnum1, register ffloat fnum2) – returns true iff $\text{fnum1} > \text{fnum2}$.

asm bool FFlgte(register ffloat fnum1, register ffloat fnum2) – returns true iff $\text{fnum1} \geq \text{fnum2}$.

asm bool FFlgtz(register ffloat fnum) – returns true iff $\text{fnum} > 0$.

asm bool FFlt(register ffloat fnum1, register ffloat fnum2) – returns true iff $\text{fnum1} < \text{fnum2}$.

asm bool FFlte(register ffloat fnum1, register ffloat fnum2) – returns true iff $\text{fnum1} \leq \text{fnum2}$.

asm bool FFltz(register ffloat fnum) – returns true iff $\text{fnum} < 0$.

asm bool FFlseqz(register ffloat fnum) – returns true iff $\text{fnum} = 0$.

Conversion functions

asm ffloat S16int2FFloat(register short int inum) – returns the ffloat equivalent of inum.

asm short int FFloatRnd2S16int(register ffloat fnum) – returns the int16 equivalent of fnum rounded up to the nearest integer.

asm short int FFloatTrunc2S16int(register ffloat fnum) – returns the int16 equivalent of fnum truncated (fractional part of fnum cut out).

asm ffloat S32int2FFloat(register long int inum) – returns the ffloat equivalent of inum.

asm ffloat U32int2FFloat(register long unsigned int unum) – returns ffloat equivalent of unum

asm ffloat IEEE2FFloat(register float fnum) – returns the ffloat equivalent of fnum.

float FFloat2IEEE(ffloat fnum) – returns the IEEE floating-point equivalent of fnum.

Other FFloat functions

asm ffloat FFneg(register ffloat fnum) – returns the negative of fnum.

asm ffloat FFabs(register ffloat fnum) – returns the absolute value of fnum.

⁹ In C, bool is not a standard type. We defined it as an unsigned char with 1 being true and 0 being false.

4.3 Cycle Count Data for FFloat Library Functions

This section lists all the functions in the FFloat Library, along with their runtimes (measured in clock cycles). Worst-case values are used (i.e. the maximum number of cycles needed to execute a function). For comparison, we calculated the runtimes for the equivalent IEEE floating-point and integer operations as well (i.e. for FFadd, we calculated the runtime for a+b twice, once when a and b were IEEE floating-point numbers, and once when a and b were integers).

The trigonometric functions (FFsin, FFcos, and FFatan) were written in C, and called other FFloat functions, so cycle counts for those functions is much higher than the cycle counts for the other functions (which were written in assembly). In addition, the FFloat2IEEE function was not tested, because it was never used in the main code (though it was used frequently during development so that we could quickly and accurately calculate the FFloat values for all our parameters).

Function Name	Cycle Count	float cycle count	int cycle count
FFadd	53	254	6
FFsub	64	264	6
FFmult	41	230	8
FFdiv	87	335	40
FFsin	1061		
FFcos	1050		
FFatan	808		
FFgt	46	157	18
FFgte	46	141	12
FFgtz	22		
FFlt	46	164	12
FFlte	46	148	12
FFltz	22		
FFeqz	21		
S16int2FFloat	22		
FFloatRnd2S16int	29		
FFloatTrunc2S16int	29		
S32int2FFloat	25		
U32int2FFloat	27		
IEEE2FFloat	50		
FFneg	35		
FFabs	35		

Table 1 Cycle Count data for FFloat library functions

The other FFloat functions are not supported by IEEE floating-point or integers in C (though the trigonometric functions are supported by IEEE floating-point numbers in C++). As shown from Table 1 above, FFloat is, on average, five times faster than IEEE floating-point, and four times slower than integers. Therefore, int operations are the fastest; however, the benefits gained from their speed is offset by the trouble needed to scale them properly.

5 Summary and Conclusion

We chose to use the FFloat (fast floating-point) numbers in the Autonomous Walking Robots project to achieve high data processing speed, wide dynamic range, and ease of software development. FFloat numbers allow us to complete a multiply operation in 41 cycles, making FFloat numbers more than ten times faster than IEEE floating-point numbers on our microprocessor. In addition, they give us an incredible 77 orders of magnitude to work with¹⁰. At the same time, FFloat numbers do not need to be scaled – the exponent part of the number takes care of scaling.

In the end, the Cornell Ranger managed to walk 1003 meters (just over a kilometer) on an indoor track unassisted (with the exception of occasional steering done remotely to prevent it from hitting the building walls. As far as we know, this is a world record for farthest distance a robot has walked on its own. The success of the Cornell Ranger could not have been realized without the use of a fast and accurate number type like FFloat.

Next semester, our team will be designing a biped (two-legged) robot. For that robot, we will be using a DSP chip with a built-in high-speed floating-point coprocessor. Therefore, we probably will not be using our FFloat library for our next robot. However, if the FFloat functions prove to be better than implementing floating-point functions on the new DSP chip, it would be worthwhile to devote more time and effort to improving the functionality and efficiency of the functions in the FFloat library.

6 Appendix A: Two's Complement

Two's Complement is a way of representing negative values in binary. Instead of representing a power of two, the top bit in a two's complement binary number is a sign bit, with 0 representing a positive number and 1 representing a negative number. Two's complement is used because it handles overflow errors without the need for special exception cases, decreasing processing times.

To find the negative of a number, we must invert all the bits in that number and add one to the result [3]. For example, starting from the 8-bit representation of 21,

0001 0101,

you can get the 8-bit representation of -21 by first inverting all the bits, as shown:

1110 1010,

then adding one to the result. The 8-bit representation of -21 would look like this:

1110 1011.

Since this process finds the two's complement (negative) of a binary number, this process works in reverse as well (going from negative to positive numbers).

¹⁰ Exponent can represent values between 2^{-128} (2.93×10^{-39}) and 2^{127} (1.70×10^{38}). Mantissa can represent values between -1 and 1.

7 Appendix B: Code for FFloat library functions

This section provides source code for all the FFloat functions. I wrote most of the comparison functions (FFgt, FFgte, FFlt, FFlte, and FFeqz¹¹) as well as a couple of the conversion functions (S16int2FFloat and S32int2FFloat). The other functions were written by Jason Cortell.

7.1 FFadd

```
asm ffloat FFadd(register ffloat ffn1,register ffloat ffn2)
{
    move.w    A0,X0          //Store ffn1 mantissa temporarily in X0
    move.w    B0,Y0          //Store ffn2 mantissa temporarily in Y0

    move.w    A1,Y1          //Put ffn1 exponent (exp1) in Y1
    sub       B,Y1           //Y1 = exp1 - exp2

//Setup: Larger ffn exponent goes in Y0; mantissa to be shifted goes in B1;
//mantissa to stay the same goes in A1; abs exp difference goes in Y1

    tlt       B,A           //Move ffn2 (mantissa and exp) to A (not
                            //shifted) if Y1 neg
    tlt       X0,B          //Move ffn1 mantissa to B1 for shifting if Y1
                            //neg
    tge       Y0,B          //Move ffn2 mantissa to B1 for shifting if Y1
                            //not negative

    abs       Y1            //positive shift values

    cmp.w     #15,Y1        //More than 15-bit shift (ASRAC only works to
                            //15 bits)?
    jgt       Neglect       //If yes, an input ffn will go to zero if
                            //shifted

    move.w    A1,Y0         //Move larger exp to Y0 for shifting
    move.w    A0,A          //Move mantissa A0 to A1 for adding

    asrac     B1,Y1,A       //Extend B1 to 36 bits, shift right by
                            //Y1, and add to A
    asr       A             //Shift right to prevent overflow of CLB (next)

    clb       A,X0          //Count sign bits
    asll.l    X0,A          //Normalize

    tst.w     A1            //Check if relevant part of result is zero
    jeq       Zero         //Result is zero

    sub       X0,Y0         //Adjust exponent of exp1
    inc.w     Y0            //Return to normal scale

    clb       Y0,X0         //check number of sign bits in exponent
    cmp.w     #8,X0         //If less than 8 (exp > 8 bits),
    jlt       Exp_Err       //jump to exponent exception handler
}
```

Continue:

¹¹ This function was originally FFeq. It was later modified to become FFeqz, FFltz, and FFgtz.

```

        rnd            A            //round to 16 bits in A1
        rtsd          //delayed return from subroutine
        move.w        A,A0         //Move mantissa of sum to lower word of ffloat
        //return value)
        move.w        Y0,A1       //Move exponent to upper word of ffloat (return
        //value)
        sxt.l         A            //Sign-extend A to 36 bits
        //end of main add function
Zero:
        rtsd          //Delayed return from subroutine - will execute
        //next three words
        move.w        #$FF80,A    //Set exp of sum to minimum
        clr.w         A0          //Set mantissa of sum to 0
        //end of zero handler
Exp_Err:
        cmp.w         #$007F,Y0   //If not overflow, go to underflow check
        jle          Underflow   //Positive or negative overflow?
        tst.w         A1         //If negative, go to negative handler
        jlt          Neg0
        move.w        #$007F,A    //Max out exponent
        rtsd          //Delayed return from subroutine - will execute
        //next three words
        move.w        #$7FFF,A0   //Max out mantissa
        nop           //Delay slot filler
        //end
Neg0:
        move.w        #$007F,A    //Max out exponent
        rtsd          //Delayed return from subroutine - will execute
        //next three cycles
        move.w        #$8000,A0   //Most negative mantissa
        nop           //Delay slot filler
        //end
Underflow:
        cmp.w        #$FF80,Y0   //Check for underflow
        jge          Continue    //Not an error
        tst.w        A1         //Positive or negative underflow?
        jlt          NegU       //If negative, go to negative handler
        move.w        #$FF80,A    //Minimum exponent
        rtsd
        move.w        #$4000,A0   //Minimum normalized positive mantissa
        nop           //Filler for third delay slot
        //end
NegU:
        move.w        #$FF80,A    //Minimum exponent
        rtsd          //Delayed return from subroutine - will execute
        //next three words
        move.w        #$BFFF,A0   //Minimum (abs) normalized negative mantissa
        nop           //filler for third delay slot
        //end of E_Err
Neglect:
        rts           //The input with the larger exp becomes the
        //output
}

```

7.2 FFsub

```

asm ffloat FFsub(register ffloat ffloat1,register ffloat ffloat2)
{

```

```

move.w    A0,X0    //Store ffnm1 mantissa temporarily in X0
move.w    B1,Y1    //Store ffnm2 mantissa temporarily in Y1

move.w    B0,B     //Prepare to negate B
asr       B        //Prevent overflow
inc.w     Y1       //Adjust exponent
neg       B        //Negate
clb      B,Y0     //Count leading bits
asll.l    Y0,B     //rescale
sub       Y0,Y1    //adjust exponent
move.w    B1,Y0
move.w    Y1,B
move.w    Y0,B0

move.w    A1,Y1    //Put ffnm1 exponent (exp1) in Y1
sub       B,Y1     //Y1 = exp1 - exp2

//Setup: Larger ffnm exponent goes in Y0; mantissa to be shifted goes in B1;
//mantissa to stay the same goes in A1; abs exp difference goes in Y1

tlt      B,A      //Move ffnm2 (mantissa and exp) to A (not
                //shifted) if Y1 neg
tlt      X0,B     //Move ffnm1 mantissa to B1 for shifting if Y1
                //neg
tge      Y0,B     //Move ffnm2 mantissa to B1 for shifting if Y1
                //not negative

abs      Y1       //positive shift values

cmp.w    #15,Y1   //More than 15-bit shift (ASRAC only works to
                //15 bits)?
jgt      Neglect  //If yes, an input ffnm will go to zero if
                //shifted

move.w    A1,Y0   //Move larger exp to Y0 for shifting
move.w    A0,A    //Move mantissa A0 to A1 for adding

asrac    B1,Y1,A  //Extend B1 to 36 bits, shift right by Y1, and
                //add to A
asr      A        //Shift right to prevent overflow of CLB (next)

clb      A,X0     //Count sign bits
asll.l    X0,A    //Normalize

tst.w    A1      //Check if relevant part of result is zero
jeq      Zero    //Result is zero

sub      X0,Y0    //Adjust exponent of exp1
inc.w    Y0      //Return to normal scale

clb      Y0,X0   //check size of exponent word
cmp.w    #8,X0
jlt      Exp_Err

Continue:
rnd      A        //Round to 16 bits
rtsd    //delayed return from subroutine

```



```

    move.w    A,A0        //Move mantissa of sum to lower word of ffloat
                        //(return value)
    move.w    Y0,A1      //Move exponent to upper word of ffloat (return
                        //value)
    sxt.l     A          //Sign-extend A to 36 bits
    //end of main add function
Zero:
    rtsd                //Delayed return from subroutine - will
                        //execute next three inst.
    move.w    #$FF80,A   //Set exp of sum to minimum
    clr.w     A0         //Set mantissa of sum to 0
    //end of zero handler
Exp_Err:
    cmp.w    #$007F,Y0
    jle      Underflow  //If not overflow, go to underflow check
    tst.w    A1         //Positive or negative overflow?
    jlt      Neg0       //If negative, go to negative handler
    move.w    #$007F,A   //Max out exponent
    rtsd                //Delayed return from subroutine - will execute
                        //next three words
    move.w    #$7FFF,A0  //Max out mantissa
    nop
    //end
Neg0:
    move.w    #$007F,A   //Max out exponent
    rtsd                //Delayed return from subroutine - will
                        //execute next three words
    move.w    #$8000,A0  //Most negative mantissa
    nop
    //end
Underflow:
    cmp.w    #$FF80,Y0  //Check for underflow
    jge      Continue   //Not an error
    tst.w    A1         //Positive or negative underflow?
    jlt      NegU       //If negative, go to negative handler
    move.w    #$FF80,A   //Minimum exponent
    rtsd                //Delayed return from subroutine - will execute
                        //next three inst.
    move.w    #$4000,A0  //Minimum normalized positive mantissa
    nop
    //end
NegU:
    move.w    #$FF80,A   //Minimum exponent
    rtsd                //Delayed return from subroutine - will execute
                        //next three inst.
    move.w    #$BFFF,A0  //Minimum (abs) normalized negative mantissa
    nop
    //end of E_Err
Neglect:
    rts                //The input with the larger exp becomes the
                        //output
}

```

7.3 FFloat

```
asm ffloat FFloat(register ffloat ffloat1, register ffloat ffloat2)
```

```
{
    move.w    B1,Y1      //This is to save exp2, use B for mult, and
                        //prepare for exp add

```

```

move.w    A0,X0    //Can't multiply A0,B0 directly
move.w    B0,Y0
mpyr      X0,Y0,B  //Multiply with round; result unlikely to
                  //differ from mpy, since truncated later
asr       B        //Shift right, so CLB can give correct count
clb       B,X0     //Count sign bits for normalization
asll.l    X0,B     //Normalize
tst.w     B1       //Check if relevant part of result is zero
jeq       Zero     //Go to zero handler
add       A,Y1     //add A1 to Y1
sub       X0,Y1    //Update exponent after normalization
inc.w     Y1       //Return to normal scale
clb       Y1,Y0    //count sign bits in exponent word
cmp.w     #8,Y0    //If <8 (exp > 8 bits),
jlt       Exp_Err //jump to exponent exception handler

Continue:
rtsd      //return with 3-cycle delay
move.w    Y1,A     //Put exp in return register
rnd       B        //Round to 16 bits in B1
move.w    B1,A0    //Move mantissa to A0
//end of mult routine

Zero:
rtsd      //return with 3-cycle delay
move.w    #$FF80,A //Set exp of sum to minimum
clr.w     A0       //Set mantissa of sum to 0
//end of zero handler

Exp_Err:
cmp.w     #$007F,Y1 //Check for overflow
jle       Underflow //If not overflow, go to underflow check
tst.w     B1       //Positive or negative overflow?
jlt       Neg0     //If negative, go to negative handler
move.w    #$7FFF,A0 //Max out mantissa
rtsd      //Delayed return - will execute next three
           //words
nop       //Filler for third delay slot
//end

Neg0:
move.w    #$007F,A //Max out exponent
rtsd      //Delayed return - will execute next three
           //words
move.w    #$8000,A0 //Most negative mantissa
nop       //Filler for third delay slot
//end

Underflow:
cmp.w     #$FF80,Y1 //Check for underflow
jge       Continue //Not an error - continue normal code
tst.w     B1       //Positive or negative overflow?
jlt       NegU     //If negative, go to negative handler
move.w    #$FF80,A //Minimum exponent
rtsd      //Delayed return - will execute next three
           //words
move.w    #$4000,A0 //Minimum normalized positive mantissa
nop       //Filler for third delay slot
//end

NegU:
move.w    #$FF80,A //Minimum exponent
rtsd      //Delayed return - will execute next three

```

```

                                //words
move.w      #$BFFF,A0      //Minimum (abs) normalized negative mantissa
nop                                //Filler for third delay slot
//end of Exp_Err
}

```

7.4 FFdiv

```

asm ffloat FFdiv(register ffloat fnum1, register ffloat fnum2)
{
    move.w    A1,X0      //Move exponent of fnum1 to X0
    move.w    B1,Y0      //Move exponent of fnum2 to Y0
    move.w    A0,Y1      //Move mantissa of fnum1 to Y1 for sign check
    move.w    A0,A       //Move mantissa of fnum1 to A1
    move.w    B0,B       //Move mantissa of fnum2 to B1
    eor.w    B,Y1        //Calculate sign of final result
                                //(sign bit of result will be 1=negative if
                                //inputs signs differ)

    abs      A
    abs      B
    jeq     DivZero      //ffnum2 cannot be zero

L1:
    cmp     A,B          //Check result of B - A
    bgt     L2           //Ready to divide
    brad    L1           //Recheck (delayed branch)
    asr     A             //Reduce fnum1 mantissa by factor of 2
    inc.w   X0           //Increase fnum1 exponent by one
    //end

L2:
    //Division of Positive Fractional Data (A1:A0 / B1)
    BFCLR   #$0001,SR    //Clear carry bit: required for 1st DIV
instruction
    //REP #16
    DIV     B1,A         //Form positive quotient in A0
    DIV     B1,A         //Form positive quotient in A0
    DIV     B1,A         //Form positive quotient in A0
    DIV     B1,A         //Form positive quotient in A0
    DIV     B1,A         //Form positive quotient in A0
    DIV     B1,A         //Form positive quotient in A0
    DIV     B1,A         //Form positive quotient in A0
    DIV     B1,A         //Form positive quotient in A0
    DIV     B1,A         //Form positive quotient in A0
    DIV     B1,A         //Form positive quotient in A0
    DIV     B1,A         //Form positive quotient in A0
    DIV     B1,A         //Form positive quotient in A0
    DIV     B1,A         //Form positive quotient in A0
    DIV     B1,A         //Form positive quotient in A0
    DIV     B1,A         //Form positive quotient in A0
    DIV     B1,A         //Form positive quotient in A0
    DIV     B1,A         //Form positive quotient in A0
    move.w   A0,A        //Move A0 to A1

    tst.w   Y1           //Check sign needed for final result
    BGE     L3           //Branch if final sign is non-neg
    NEG     A             //Negate mantissa if result is neg

L3:
    clb     A,Y1         //Count sign bits

```

```

        asll.l    Y1,A        //Normalize

        tst      A           //Check if relevant part of result is zero
        jeq     Zero        //Result is zero

        sub     Y0,X0        //Adjust exponent of expl
        sub     Y1,X0

        clb     X0,Y0        //check size of exponent word
        cmp.w   #8,Y0
        jlt     Exp_Err

Continue:
        RTSD
        MOVE.W   A,A0
        MOVE.W   X0,A1
        sxt.l   A           //Sign-extend A to 36 bits
        //END

DivZero:
        //Call error handler here
        MOVE.W   #$007F,A    //Needs work here
        RTSD
        MOVE.W   #$7FFF,A0
        NOP
        //END

Zero:
        RTSD
        MOVE.W   #$FF80,A
        CLR.W   A0
        //END

Exp_Err:
        cmp.w   #$007F,X0
        jle     Underflow    //If not overflow, go to underflow check
        tst.w   A1           //Positive or negative overflow?
        jlt     Neg0         //If negative, go to negative handler
        move.w  #$007F,A     //Max out exponent
        rtsd                //Delayed return from subroutine - will
                            //execute next three words

        move.w  #$7FFF,A0    //Max out mantissa
        nop
        //end

Neg0:
        move.w  #$007F,A     //Max out exponent
        rtsd                //Delayed return from subroutine - will
                            //execute next three words

        move.w  #$8000,A0    //Most negative mantissa
        nop                 //filler for third delay slot
        //end

Underflow:
        cmp.w   #$FF80,X0    //Check for underflow
        jge     Continue     //Not an error
        tst.w   A1           //Positive or negative underflow?
        jlt     NegU         //If negative, go to negative handler
        move.w  #$FF80,A     //Minimum exponent
        rtsd                //Delayed return from subroutine - will
                            //execute next three words

        move.w  #$4000,A0    //Minimum normalized positive mantissa
        nop                 //Filler for third delay slot

```

```

        //end
NegU:
    move.w    #$FF80,A    //Minimum exponent
    rtsd      //Delayed return from subroutine - will
                //execute next three words
    move.w    #$BFFF,A0  //Minimum (abs) normalized negative mantissa
    nop      //filler for third delay slot
    //end of E_Err
}

```

7.5 FFsin

```

ffloat FFsin(ffloat xin)
{
    int k,klo,khi;
    ffloat xdiff0, xdiff1;
    ffloat x=xin;
static ffloat xlo = 0x00029b78;
static ffloat xhi = 0x00026487;
static ffloat ya[31] = {0xffccb968, 0xfffe958c, 0xffff97e0, 0x0000b4c3,
0x0000a0e0, 0x00009126, 0x00008643, 0x000080b3, 0x000080b3, 0x00008643,
0x00009126, 0x0000a0e0, 0x0000b4c3, 0xffff97e0, 0xfffe958c, 0xff800000,
0xfffe6a73, 0xffff681f, 0x00004b3c, 0x00005f1f, 0x00006ed9, 0x000079bc,
0x00007f4c, 0x00007f4c, 0x000079bc, 0x00006ed9, 0x00005f1f, 0x00004b3c,
0xffff681f, 0xfffe6a73, 0xffcc4698};

static ffloat y2a[31] = {0xff800000, 0xfffd6a0f, 0xfffe67be, 0xffff4af6,
0xffff5ec6, 0xffff6e72, 0xffff794a, 0xffff7ed5, 0xffff7ed5, 0xffff794a,
0xffff6e72, 0xffff5ec6, 0xffff4af6, 0xfffe67be, 0xfffd6a0f, 0xff800000,
0xfffd95f0, 0xfffe9841, 0xffffb509, 0xfffffa139, 0xffff918d, 0xffff86b5,
0xffff812a, 0xffff812a, 0xffff86b5, 0xffff918d, 0xfffffa139, 0xffffb509,
0xfffe9841, 0xfffd95f0, 0xfffd95f0};

static int numpoints = 31;
static ffloat h = 0xfffe6b3b;
static ffloat hinv = 0x00034c64;
static ffloat pi2=0x00036487;
static ffloat pi2inv=0xfffe517c;

if(FFlt(xin,xlo)){
    x=FFadd(
        xin,
        FFmult(
            S16int2FFloat(
                FFfloatTrunc2S16int(
                    FFmult(
                        FFsub(xhi,xin),
                        pi2inv
                    )
                )
            ),
            pi2
        )
    );
}else if(FFgt(xin,xhi)){
    x=FFsub(
        xin,
        FFmult(

```

```

    S16int2FFloat(
    FFloatTrunc2S16int(
        FFloatTrunc2S16int(
            FFmult(
                FFsub(xin,xlo),
                pi2inv
            )
        )
    ),
    pi2
)
);
}
klo = FFloatTrunc2S16int(FFmult(FFsub(x,xlo),hinv));
khi=klo+1;
xdiff0 = FFsub(x, FFadd(xlo, FFmult(h,S16int2FFloat(klo))));
xdiff1 = FFsub(xdiff0, h);
return ( FFadd(ya[klo], FFadd(FFmult(FFmult(FFsub(ya[khi],ya[klo])),
    hinv), xdiff0), FFmult(FFmult(y2a[khi], xdiff0), xdiff1))) );
}

```

7.6 FFCos

```

ffloat FFCos(ffloat xin)
{
    int k,klo,khi;
    ffloat xdiff0, xdiff1;
    ffloat x=xin;
static ffloat xlo = 0x00029b78;
static ffloat xhi = 0x00026487;
static ffloat ya[31] = {0x00008000, 0x000082cc, 0x00008b10, 0x00009872,
0x0000aa59, 0xffff8000, 0xffffb0e4, 0xfffd94f6, 0xfffd6b09, 0xffff4f1b,
0x00004000, 0x000055a6, 0x0000678d, 0x000074ef, 0x00007d33, 0x00014000,
0x00007d33, 0x000074ef, 0x0000678d, 0x000055a6, 0x00004000, 0xffff4f1b,
0xfffd6b09, 0xfffd94f6, 0xffffb0e4, 0xffff8000, 0x0000aa59, 0x00009872,
0x00008b10, 0x000082cc, 0x00008000};

static ffloat y2a[31] = {0xff800000, 0xffff7cbe, 0xffff7481, 0xffff672d,
0xffff5556, 0xfffe7f88, 0xfffe4ed1, 0xfffc6aa5, 0xfffc955a, 0xfffeb12e,
0xfffe8077, 0xffffaaa9, 0xffff98d2, 0xffff8b7e, 0xffff8341, 0xfffeb12e,
0xffff8341, 0xffff8b7e, 0xffff98d2, 0xffffaaa9, 0xfffe8077, 0xfffeb12e,
0xfffc955a, 0xfffc6aa5, 0xfffe4ed1, 0xfffe7f88, 0xffff5556, 0xffff672d,
0xffff7481, 0xffff7cbe, 0xffff7cbe};

static int numpoints = 31;
static ffloat h = 0xfffe6b3b;
static ffloat hinv = 0x00034c64;
static ffloat pi2=0x00036487;
static ffloat pi2inv=0xfffe517c;

if(FFlt(xin,xlo)){
    x=FFadd(
        xin,
        FFmult(
            S16int2FFloat(
            FFloatTrunc2S16int(
                FFmult(
                    FFsub(xhi,xin),
                    pi2inv
                )
            )
        )
    )
}

```

```

        )
        )
    ),
    pi2
)
);
}else if(FFgt(xin,xhi)){
    x=FFsub(
        xin,
        FFMult(
            S16int2FFloat(
                FFloatTrunc2S16int(
                    FFMult(
                        FFsub(xin,xlo),
                        pi2inv
                    )
                )
            ),
            pi2
        )
    );
}
klo = FFloatTrunc2S16int(FFmult(FFsub(x,xlo),hinv));
khi=klo+1;
xdiff0 = FFsub(x, FFadd(xlo, FFMult(h,S16int2FFloat(klo))));
xdiff1 = FFsub(xdiff0, h);
return ( FFadd(ya[klo], FFadd(FFmult(FFmult(FFsub(ya[khi],ya[klo])),
    hinv), xdiff0), FFMult(FFmult(y2a[khi], xdiff0), xdiff1))) );
}

```

7.7 FFatan

```

ffloat FFatan(ffloat xin)
{
    int k,klo,khi;
    ffloat xdiff0, xdiff1;
    ffloat x=xin;
    static ffloat xlo = 0x0005b000;
    static ffloat xhi = 0x00055000;
    static ffloat ya[151] = {0x00019eaa, 0x00019eb5, 0x00019ec0, 0x00019ecc,
    0x00019ed8, 0x00019ee4, 0x00019ef1, 0x00019efe, 0x00019f0c, 0x00019f19,
    0x00019f28, 0x00019f36, 0x00019f46, 0x00019f55, 0x00019f66, 0x00019f76,
    0x00019f88, 0x00019f99, 0x00019fac, 0x00019fbf, 0x00019fd3, 0x00019fe8,
    0x00019ffd, 0x0001a013, 0x0001a02a, 0x0001a042, 0x0001a05b, 0x0001a075,
    0x0001a090, 0x0001a0ac, 0x0001a0ca, 0x0001a0e9, 0x0001a109, 0x0001a12b,
    0x0001a14e, 0x0001a173, 0x0001a19a, 0x0001a1c3, 0x0001a1ee, 0x0001a21c,
    0x0001a24c, 0x0001a27f, 0x0001a2b5, 0x0001a2ef, 0x0001a32c, 0x0001a36d,
    0x0001a3b3, 0x0001a3fd, 0x0001a44d, 0x0001a4a2, 0x0001a4ff, 0x0001a563,
    0x0001a5d0, 0x0001a646, 0x0001a6c7, 0x0001a754, 0x0001a7f0, 0x0001a89d,
    0x0001a95d, 0x0001aa33, 0x0001ab25, 0x0001ac37, 0x0001ad71, 0x0001aeda,
    0x0001b07f, 0x0001b26e, 0x0001b4bc, 0x0001b785, 0x0001baf1, 0x0001bf38,
    0x0000894e, 0x00009757, 0x0000a9a2, 0xffff8292, 0xffffbd49, 0xff800000,
    0xffff42b6, 0xffff7d6d, 0x0000565d, 0x000068a8, 0x000076b1, 0x000140c7,
    0x0001450e, 0x0001487a, 0x00014b43, 0x00014d91, 0x00014f80, 0x00015125,
    0x0001528e, 0x000153c8, 0x000154da, 0x000155cc, 0x000156a2, 0x00015762,
    0x0001580f, 0x000158ab, 0x00015938, 0x000159b9, 0x00015a2f, 0x00015a9c,
    0x00015b00, 0x00015b5d, 0x00015bb2, 0x00015c02, 0x00015c4c, 0x00015c92,
    0x00015cd3, 0x00015d10, 0x00015d4a, 0x00015d80, 0x00015db3, 0x00015de3,

```

```

0x00015e11, 0x00015e3c, 0x00015e65, 0x00015e8c, 0x00015eb1, 0x00015ed4,
0x00015ef6, 0x00015f16, 0x00015f35, 0x00015f53, 0x00015f6f, 0x00015f8a,
0x00015fa4, 0x00015fbd, 0x00015fd5, 0x00015fec, 0x00016002, 0x00016017,
0x0001602c, 0x00016040, 0x00016053, 0x00016066, 0x00016077, 0x00016089,
0x00016099, 0x000160aa, 0x000160b9, 0x000160c9, 0x000160d7, 0x000160e6,
0x000160f3, 0x00016101, 0x0001610e, 0x0001611b, 0x00016127, 0x00016133,
0x0001613f, 0x0001614a, 0x00016155};

```

```

static ffloat y2a[151] = {0xff800000, 0xffff443e4, 0xffff446b6, 0xffff449b0,
0xffff44cd5, 0xffff45029, 0xffff453af, 0xffff4576a, 0xffff45b5f, 0xffff45f92,
0xffff46408, 0xffff468c6, 0xffff46dd1, 0xffff47331, 0xffff478ec, 0xffff47f0a,
0xffff542c9, 0xffff54648, 0xffff54a06, 0xffff54e0a, 0xffff55259, 0xffff556fa,
0xffff55bf6, 0xffff56156, 0xffff56722, 0xffff56d66, 0xffff5742f, 0xffff57b8a,
0xffff641c3, 0xffff6461c, 0xffff64ad8, 0xffff65004, 0xffff655ac, 0xffff65be0,
0xffff662b0, 0xffff66a30, 0xffff67278, 0xffff67ba1, 0xffff742e5, 0xffff7488b,
0xffff74ed9, 0xffff755e6, 0xffff75dd0, 0xffff766ba, 0xffff770cc, 0xffff77c39,
0xffff8449e, 0xffff84c0f, 0xffff8549c, 0xffff85e7b, 0xffff869ef, 0xffff8774e,
0xffff9437f, 0xffff94cc5, 0xffff957cc, 0xffff96504, 0xffff974fc, 0xffffa4439,
0xffffa5032, 0xffffa5f16, 0xffffa71cd, 0xffffb44d0, 0xffffb542e, 0xffffb684a,
0xffffc4182, 0xffffc538f, 0xffffc6c5c, 0xffffd4779, 0xffffd5fe2, 0xffffe4133,
0xffffe5918, 0xffffe77b6, 0xfffff4b62, 0xfffff503a, 0xffffe707d, 0xff800000,
0xffffe8f82, 0xfffffafc5, 0xfffffb49d, 0xffffe8849, 0xffffea6e7, 0xffffebecc,
0xffffda01d, 0xffffdb886, 0xffffc93a3, 0xffffcac70, 0xffffcbe7d, 0xffffb97b5,
0xffffbabd1, 0xffffbbb2f, 0xffffa8e32, 0xffffaa0e9, 0xffffaafcd, 0xffffabbc6,
0xffff98b03, 0xffff99afb, 0xffff9a833, 0xffff9b33a, 0xffff9bc80, 0xffff888b1,
0xffff89610, 0xffff8a184, 0xffff8ab63, 0xffff8b3f0, 0xffff8bb61, 0xffff783c6,
0xffff78f33, 0xffff79945, 0xffff7a22f, 0xffff7aa19, 0xffff7b126, 0xffff7b774,
0xffff7bd1a, 0xffff6845e, 0xffff68d87, 0xffff695cf, 0xffff69d4f, 0xffff6a41f,
0xffff6aa53, 0xffff6affb, 0xffff6b527, 0xffff6b9e3, 0xffff6be3c, 0xffff58475,
0xffff58bd0, 0xffff59299, 0xffff598dd, 0xffff59ea9, 0xffff5a409, 0xffff5a905,
0xffff5ada6, 0xffff5b1f5, 0xffff5b5f9, 0xffff5b9b7, 0xffff5bd36, 0xffff480f5,
0xffff48713, 0xffff48cce, 0xffff4922e, 0xffff49739, 0xffff49bf7, 0xffff4a06d,
0xffff4a4a0, 0xffff4a895, 0xffff4ac50, 0xffff4afd6, 0xffff4b32a, 0xffff4b64f,
0xffff4b949, 0xffff4bc1b, 0xffff4bc1b};

```

```

static int numpoints = 151;
static ffloat h = 0xffff4444;
static ffloat hinv = 0x00027800;
    klo = FFloatTrunc2S16int(FFmult(FFsub(x,xlo),hinv));
    khi=klo+1;

if(FFlt(x,xlo)){
    return(ya[0]);
}else if(FFgt(x,xhi)){
    return(ya[numpoints-1]);
}

xdiff0 = FFsub(x, FFadd(xlo, FFmult(h,S16int2FFloat(klo))));
xdiff1 = FFsub(xdiff0, h);
return ( FFadd(ya[klo], FFadd(FFmult(FFmult(FFsub(ya[khi],ya[klo]),
    hinv), xdiff0), FFmult(FFmult(y2a[khi], xdiff0), xdiff1))) );
}

```

7.8 FFgt

```

//return true if ffnun1>ffnum2, false otherwise
asm bool FFgt(register ffloat ffnun1, register ffloat ffnun2)
{
    //First compare signs of numbers

```



```

tst.w A0
blt      CheckSignANeg

//a is nonnegative
tst.w B0
//Both numbers are nonnegative - nonnegative exponents case
bge      CasePNumExp
//If b is negative, a>b
rtsd
move.w   #1,Y0
nop
nop

//a is negative
CheckSignANeg:
tst.w B0
//Both numbers are negative - negative exponents case
blt      CaseNNumExp
//If b is nonnegative, a<b
rtsd
move.w   #0,Y0
nop
nop

//If a and b are positive, go here
//larger exponent = larger #
CasePNumExp:
//move exponent data to X0 and Y0 registers for comparison
move.w   A1,X0
move.w   B1,Y0
cmp.w    X0,Y0
blt      aGTb           //if(expB<expA) then a>b
bgt      aNotGTb       //if(expB>expA) then !(a>b)

//If exponents are equal, check mantissas
move.w   A0,X0
move.w   B0,Y0
cmp.w    X0,Y0
blt      aGTb           //if(mantissaB<mantissaA) then a>b
rtsd
move.w   #0,Y0
nop
nop

//If a and b are negative, go here
//larger exponent = smaller #
CaseNNumExp:
//move exponent data to X0 and Y0 registers for comparison
move.w   A1,X0
move.w   B1,Y0
cmp.w    X0,Y0
bgt      aGTb           //if(expB>expA) then a>b
blt      aNotGTb       //if(expB<expA) then !(a>b)

//If exponents are equal, check mantissas
move.w   A0,X0
move.w   B0,Y0
cmp.w    X0,Y0

```

```

        blt          aGTb          //if(mantissaB<mantissaA) then a>b
        rtsd
        move.w      #0,Y0
        nop
        nop

//if a>b, go here
aGTb:
        rtsd
        move.w      #1,Y0
        nop
        nop

//if a<=b, go here
aNotGTb:
        rtsd
        move.w      #0,Y0
        nop
        nop
}

```

7.9 FFgte

```

//return true if a>=b, false otherwise
asm bool FFgte(register ffloat a, register ffloat b)
{
    //First compare signs of numbers
    tst.w A0
    blt          CheckSignANeg

    //a is nonnegative
    tst.w B0
    //Both numbers are nonnegative - nonnegative exponents case
    bge          CasePNumExp
    //If b is negative, a>=b
    rtsd
    move.w      #1,Y0
    nop
    nop

//a is negative
CheckSignANeg:
    tst.w B0
    //Both numbers are negative - negative exponents case
    blt          CaseNNumExp
    //If b is nonnegative, a<b
    rtsd
    move.w      #0,Y0
    nop
    nop

//If a and b are positive, go here
//larger exponent = larger #
CasePNumExp:
    //move exponent data to X0 and Y0 registers for comparison
    move.w      A1,X0
    move.w      B1,Y0

```

```

cmp.w      X0,Y0
blt       aGTEb      //if(expB<expA) then a>=b
bgt       aNotGTEb   //if(expB>expA) then !(a>=b)

//If exponents are equal, check mantissas
move.w    A0,X0
move.w    B0,Y0
cmp.w    X0,Y0
ble      aGTEb      //if(mantissaB<=mantissaA) then a>=b
rtsd
move.w    #0,Y0
nop
nop

//If a and b are negative, go here
//larger exponent = smaller #
CaseNNumExp:
//move exponent data to X0 and Y0 registers for comparison
move.w    A1,X0
move.w    B1,Y0
cmp.w    X0,Y0
bgt      aGTEb      //if(expB>expA) then a>b
blt      aNotGTEb   //if(expB<expA) then !(a>b)

//If exponents are equal, check mantissas
move.w    A0,X0
move.w    B0,Y0
cmp.w    X0,Y0
ble      aGTEb      //if(mantissaB<=mantissaA) then a>=b
rtsd
move.w    #0,Y0
nop
nop

//if a>=b, go here
aGTEb:
rtsd
move.w    #1,Y0
nop
nop

//if a<b, go here
aNotGTEb:
rtsd
move.w    #0,Y0
nop
nop
}

```

7.10 FFgtz

```

asm bool FFgtz(register ffloat fnum)
{
//Test fnum mantissa
tst.w    A0
bgt      Positive

//fnum <= 0

```

```

    rtsd                //delayed return
    clr.w Y0            //return value 0
    nop                 //first filler instruction
    nop                 //second filler instruction
    //end

Positive:
    //ffnum > 0
    rtsd                //delayed return
    move.w #1,Y0        //return value 1
    nop                 //first filler instruction
    nop                 //second filler instruction
    //end
}

//return true if ffnum<0, false otherwise
asm bool FFltz(register ffloat ffnum)
{
    //Test ffnum mantissa
    tst.w A0
    blt Negative

    //ffnum >= 0
    rtsd                //delayed return
    clr.w Y0            //return value 0
    nop                 //first filler instruction
    nop                 //second filler instruction
    //end

Negative:
    //ffnum < 0
    rtsd                //delayed return
    move.w #1,Y0        //return value 1
    nop                 //first filler instruction
    nop                 //second filler instruction
    //end
}

```

7.11 FFlt

```

//return true if ffnum1<ffnum2, false otherwise
asm bool FFlt(register ffloat ffnum1, register ffloat ffnum2)
{
    //First compare signs of numbers
    tst.w A0
    blt CheckSignANeg

    //a is nonnegative
    tst.w B0
    //Both numbers are nonnegative - nonnegative exponents case
    bge CasePNumExp
    //If b is negative, !(a<b)
    rtsd
    move.w #0,Y0
    nop
    nop

    //a is negative

```

```

CheckSignANeg:
    tst.w B0
    //Both numbers are negative - negative exponents case
    blt      CaseNNumExp
    //If b is nonnegative, a<b
    rtsd
    move.w   #1,Y0
    nop
    nop

//If a and b are positive, go here
//larger exponent = larger #
CasePNumExp:
    //move exponent data to X0 and Y0 registers for comparison
    move.w   A1,X0
    move.w   B1,Y0
    cmp.w    X0,Y0
    bgt      aLTb           //if(expB>expA) then a<b
    blt      aNotLTb       //if(expB<expA) then !(a<b)

    //If exponents are equal, check mantissas
    move.w   A0,X0
    move.w   B0,Y0
    cmp.w    X0,Y0
    bgt      aLTb           //if(mantissaB>mantissaA) then a<b
    rtsd
    move.w   #0,Y0
    nop
    nop

//If a and b are negative, go here
//larger exponent = smaller #
CaseNNumExp:
    //move exponent data to X0 and Y0 registers for comparison
    move.w   A1,X0
    move.w   B1,Y0
    cmp.w    X0,Y0
    blt      aLTb           //if(expB<expA) then a<b
    bgt      aNotLTb       //if(expB>expA) then !(a<b)

    //If exponents are equal, check mantissas
    move.w   A0,X0
    move.w   B0,Y0
    cmp.w    X0,Y0
    bgt      aLTb           //if(mantissaB>mantissaA) then a<b
    rtsd
    move.w   #0,Y0
    nop
    nop

//if a<b, go here
aLTb:
    rtsd
    move.w   #1,Y0
    nop
    nop

//if a>=b, go here

```

```

aNotLTb:
    rtsd
    move.w    #0,Y0
    nop
    nop
}

```

7.12 FFfte

```

//return true if a<=b, false otherwise
asm bool FFfte(register ffloat a, register ffloat b)
{
    //First compare signs of numbers
    tst.w A0
    blt      CheckSignANeg

    //a is nonnegative
    tst.w B0
    //Both numbers are nonnegative - nonnegative exponents case
    bge      CasePNumExp
    //If b is negative, !(a<=b)
    rtsd
    move.w    #0,Y0
    nop
    nop

//a is negative
CheckSignANeg:
    tst.w B0
    //Both numbers are negative - negative exponents case
    blt      CaseNNumExp
    //If b is nonnegative, a<b
    rtsd
    move.w    #1,Y0
    nop
    nop

//If a and b are positive, go here
//larger exponent = larger #
CasePNumExp:
    //move exponent data to X0 and Y0 registers for comparison
    move.w    A1,X0
    move.w    B1,Y0
    cmp.w     X0,Y0
    bgt      aLTeb      //if(expB>expA) then a<=b
    blt      aNotLTeb   //if(expB>expA) then !(a<=b)

    //If exponents are equal, check mantissas
    move.w    A0,X0
    move.w    B0,Y0
    cmp.w     X0,Y0
    bge      aLTeb      //if(mantissaB>=mantissaA) then a>=b
    rtsd
    move.w    #0,Y0
    nop
    nop
}

```

```

//If a and b are negative, go here
//larger exponent = smaller #
CaseNNumExp:
    //move exponent data to X0 and Y0 registers for comparison
    move.w    A1,X0
    move.w    B1,Y0
    cmp.w     X0,Y0
    blt      aLTeb        //if(expB<expA) then a<=b
    bgt      aNotLTeb     //if(expB>expA) then !(a<=b)

    //If exponents are equal, check mantissas
    move.w    A0,X0
    move.w    B0,Y0
    cmp.w     X0,Y0
    bge      aLTeb        //if(mantissaB>=mantissaA) then a>=b
    rtsd
    move.w    #0,Y0
    nop
    nop

//if a<=b, go here
aLTeb:
    rtsd
    move.w    #1,Y0
    nop
    nop

//if a>b, go here
aNotLTeb:
    rtsd
    move.w    #0,Y0
    nop
    nop
}

```

7.13 FFltz

```

asm bool FFltz(register ffloat ffnun)
{
    //Test ffnun mantissa
    tst.w     A0
    blt      Negative

    //ffnum >= 0
    rtsd                      //delayed return
    clr.w     Y0              //return value 0
    nop                      //first filler instruction
    nop                      //second filler instruction
    //end

Negative:
    //ffnum < 0
    rtsd                      //delayed return
    move.w    #1,Y0          //return value 1
    nop                      //first filler instruction
    nop                      //second filler instruction
    //end
}

```

```

asm bool FFeqz(register ffloat fnum)
{
    //Test fnum mantissa
    tst.w      A0
    beq        Zero

    //ffnum != 0
    rtsd
    clr.w      Y0          //delayed return
                        //return value 0
    nop
    nop          //first filler instruction
    nop          //second filler instruction
    //end

Zero:
    //ffnum < 0
    rtsd
    move.w     #1,Y0      //delayed return
                        //return value 1
    nop
    nop          //first filler instruction
    nop          //second filler instruction
    //end
}

```

7.14 FFeqz

//return true if fnum=0, false otherwise
asm bool FFeqz(register ffloat fnum)

```

{
    //Test fnum mantissa
    tst.w A0
    beq        Zero

    //ffnum != 0
    rtsd
    clr.w Y0
    nop
    nop

Zero:
    //ffnum < 0
    rtsd
    move.w     #1,Y0      //return value 1
    nop
    nop
}

```

7.15 S16int2FFloat

//convert an int16 to an ffloat value
asm ffloat S16int2FFloat(register short int inum)

```

{
    tst.w Y0
    jeq        Zero

    //inum != 0
    clb        Y0,X0
    asll.l     X0,Y0      //normalize inum
    neg        X0          //set exponent
    rtsd
}

```



```

        add.w      #15,X0
        move.w    X0,A          //exponent
        move.w    Y0,A0       //mantissa

//FFloat zero = 0xFF800000
Zero:
        rtsd
        move.w    #$FF80,A
        clr.w    A0
}

```

7.16 S32int2FFloat

```

//convert an int32 to an ffloat value
asm ffloat S32int2FFloat(long int inum)
{
    //inum = 0
    tst        A
    jeq        Zero

    //inum != 0
    clb        A,X0
    asll.l     X0,A          //normalize inum
    neg        X0          //set exponent
    add.w      #31,X0
    rnd        A
    rtsd
    move.w     A1,A0 //mantissa
    move.w     X0,A1 //exponent
    sxt.l     A          //sign-extend A to 36 bits

//FFloat zero = 0xFF800000
Zero:
    rtsd
    move.w     #$FF80,A
    clr.w     A0
}

```

7.17 U32int2FFloat

```

//convert an unsigned int32 to an ffloat value
asm ffloat U32int2FFloat(long unsigned int unum)
{
    tst        A
    jeq        Zero          //unum = 0
    jlt        LongUnsigned //If 2^31 <= unum <= 2^32-1, unum will
                            //be a negative number

    //unum <= 2^31 - 1
    clb        A,X0
    asll.l     X0,A          //normalize unum
    neg        X0          //set exponent
    add.w      #31,X0
    rtsd
    move.w     A1,A0 //mantissa
    move.w     X0,A1 //exponent
    sxt.l     A          //sign-extend A to 36 bits
}

```

```

//FFloat zero = 0xFF800000
Zero:
    rtsd
    move.w    #$FF80,A
    clr.w     A0

//If unum is between 2^31 and 2^32-1
LongUnsigned:
    lsr.w     A           //divide mantissa by 2
    move.w    A1,A0      //move mantissa to its right place

    //divide the mantissa by two and increase the exponent by 1
    //this will correct the sign of A while keeping the absolute
    //value of a the same
    rtsd
    move.w    #32,A1     //exponent will always be 32 for this case
    sxt.l     A          //sign-extend A to 36 bits
}

```

7.18 FFloatRnd2S16int

```

asm short int FFloatRnd2S16int(register ffloat ffnun)
{
    move.w    A1,Y0
    move.w    A0,A

    //Scale so that exponent = 15; converts mantissa to integer scale
    //Check if resulting mantissa is in range -32768 to 32767 (16 bit
    //signed int)
    sub.w     #15,Y0
    jgt       Over           //Number is outside range -32768 to 32767
    cmp.w     #-17,Y0
    jlt       Zero          //Number is small and rounds to zero
    rtsd
    asll.l    Y0,A          //Scale to exponent = 15 (one word, two cycles)
    rnd       A             //Convergent rounding (round down boundary case
    //if even)

    move.w    A1,Y0
    //end

Zero:
    rtsd
    clr.w     Y0           //Result is zero
    nop
    nop
    //end

Over:
    tst       A
    blt       Neg          //branch to Neg: if number is below 32768
    rtsd
    move.w    #$7FFF,Y0    //Set to most positive 16-bit value
    nop          //Filler for third delay slot
    //end

Neg:

```

```

    rtsd
    move.w    #$8000,Y0        //Set to most negative 16-bit value
    nop      //Filler for third delay slot
    //end
}

```

7.19 FFloatTrunc2S16int

```

asm short int FFloatTrunc2S16int(register ffloat fnum)
{
    move.w    A1,Y0
    move.w    A0,A

    //Scale so that exponent = 15; converts mantissa to integer scale
    //Check if resulting mantissa is in range -32768 to 32767 (16 bit signed int)
    sub.w    #15,Y0
    jgt      Over            //Number is outside range -32768 to 32767
    cmp.w    #-17,Y0
    jlt      Zero           //Number is small and rounds to zero
    rtsd
    asll.l   Y0,A           //Scale to exponent = 15 (one word, two cycles)
    move.w    A1,Y0
    nop      //Filler for third delay slot
    //end

Zero:
    rtsd
    clr.w    Y0            //Result is zero
    nop
    nop
    //end

Over:
    tst      A
    blt     Neg           //branch to Neg: if number is below -32768
    rtsd
    move.w   #$7FFF,Y0    //Set to most positive 16-bit value
    nop     //Filler for third delay slot
    //end

Neg:
    rtsd
    move.w   #$8000,Y0    //Set to most negative 16-bit value
    nop     //Filler for third delay slot
    //end
}

```

7.20 IEEE2FFloat

```

asm ffloat IEEE2FFloat(register float fnum)
{
    bftstl   #$7F80,A1
    jcs     Zero            //For IEEE, zero is indicated by zero exp.

    move.w   A1,Y0
    bfclr   #$FF00,A1
    sxt.l   A                //Sign-extend A to 36 bits
    bfset   #$0080,A1
}

```

```

        brclr    #$8000,Y0,L1    //Branch if sign bit is positive
        neg     A                //Negate mantissa if sign bit is negative
L1:
        clb     A,X0            //Normalize mantissa
        asll.l  X0,A

        bfclr   #$807F,Y0
        lsrr.w  #7,Y0
        sub.w   #119,Y0
        sub     X0,Y0           //FFloat exponent is ready
        clb     Y0,X0          //Check for overflow/underflow
        cmp.w   #8,X0
        jlt     Exp_Err

Continue:
        rnd     A
        rtsd
        move.w  A,A0
        move.w  Y0,A1
        sxt.l  A                //Sign-extend A to 36 bits
        //end

Zero:
        RTSD
        MOVE.W  #$FF80,A
        CLR.W  A0
        //END

Exp_Err:
        cmp.w   #$007F,Y0
        jle     Underflow      //If not overflow, go to underflow check
        tst.w   A1             //Positive or negative overflow?
        jlt     Neg0           //If negative, go to negative handler
        move.w  #$007F,A       //Max out exponent
        rtsd                  //Delayed return from subroutine - will
                               //execute next three words

        move.w  #$7FFF,A0      //Max out mantissa
        nop                    //filler for third delay slot
        //end

Neg0:
        move.w  #$007F,A       //Max out exponent
        rtsd                  //Delayed return from subroutine - will
                               //execute next three words

        move.w  #$8000,A0      //Most negative mantissa
        nop                    //filler for third delay slot
        //end

Underflow:
        cmp.w   #$FF80,Y0     //Check for underflow
        jge     Continue      //Not an error
        tst.w   A1             //Positive or negative underflow?
        jlt     NegU
        move.w  #$FF80,A       //Minimum exponent
        rtsd                  //Delayed return from subroutine - will
                               //execute next three words

        move.w  #$4000,A0      //Minimum normalized positive mantissa
        nop                    //Filler for third delay slot
        //end

NegU:
        move.w  #$FF80,A       //Minimum exponent

```

```

rtsd                                //Delayed return from subroutine - will
                                     //execute next three words
move.w    #$BFFF,A0                 //Minimum (abs) normalized negative
                                     //mantissa
nop                                     //filler for third delay slot
//end of E_Err
}

```

7.21 FFloat2IEEE

```

float FFloat2IEEE(ffloat fnum)
{
    float fout = 0;
    long int iexp = 0;
    long unsigned int tempout = 0, sign = 0, mantissa = 0, exp = 0;
    void *VoidPointer;
    float *FloatPointer;
    long unsigned int *LintPointer;

    if (ffnum&0xFFFF) //ffnum is not zero
    {
        mantissa = fnum & 0x0000FFFF;

        exp = fnum&0xFFFF0000;
        iexp = (long int)exp;

        iexp += 0x007F0000;           //Bias exponent positive by 127

        if (iexp < 0x00010000)       //Limit exponent size to allowed
                                     //IEEE range
        {
            iexp = 0x00010000;
        }
        else if (iexp > 0x00FE0000)
        {
            iexp = 0x00FE0000;
        }

        if (mantissa&0x00008000)     //ffnum is negative
        {
            sign = 0x80000000;
            mantissa ^= 0x0000FFFF; //Negate
            mantissa++;
        }

        while (!(mantissa&0x8000))   //normalize
        {
            mantissa <<= 1;
            iexp -= 0x00010000;
        }

        if (iexp < 0x00010000)       //Limit exponent size to allowed
                                     //IEEE range
        {
            iexp = 0x00010000;
        }
        else if (iexp > 0x00FE0000)
    }
}

```

```

    {
        iexp = 0x00FE0000;
    }

    exp = (long unsigned int)iexp;

    exp <<= 7;           //Shift exponent to correct position

    mantissa <<= 8;      //Shift to correct IEEE position
    mantissa &= 0x007FFFFFFF; //Clear leading one

    tempout = sign | exp | mantissa;
}
else exp = 0x00000000;           //zero

VoidPointer = &(tempout);        //obtain pointer to unsigned long
                                   //int tempout
FloatPointer = VoidPointer;      //convert to float
fout = *FloatPointer;
return(fout);
}

```

7.22 FFneg

```

asm ffloat FFneg(register ffloat ffnun)
{
    move.w    A1,Y0           //store ffnun exp in Y0
    move.w    A0,A           //A holds mantissa of ffnun
    neg       A              //full 36-bit negate
    asr       A              //shift right to prevent overflow of clb
    jeq       Zero          //Don't normalize if zero

    //ffnum != 0
    clb       A,X0           //Count sign bits
    asll.l    X0,A           //Normalize

    sub       X0,Y0         //Adjust exponent
    inc.w     Y0            //Return to normal scale

    clb       Y0,X0         //check number of sign bits in exponent
    cmp.w     #8,X0         //If less than 8 (exp > 8 bits),
    jlt       Exp_Err       //jump to exponent exception handler

Continue:
    rtsd           //delayed return from subroutine
    move.w     A1,A0        //Move mantissa of sum to lower word of ffnun1
                                   //(return value)
    move.w     Y0,A1        //Move exponent to upper word of ffnun1 (return
                                   //value)
    sxt.l     A            //Sign-extend A to 36 bits
    //end of main neg function

Zero:
    rtsd           //Delayed return from subroutine - will
                                   execute next three words
    move.w     #$FF80,A     //Set exp of sum to minimum
    clr.w     A0           //Set mantissa of sum to 0
    //end of zero handler

```

```

Exp_Err:
    cmp.w    #$007F,Y0
    jle     Underflow    //If not overflow, go to underflow check
    tst.w   A1           //Positive or negative overflow?
    jlt     NegO         //If negative, go to negative handler
    move.w  #$007F,A     //Max out exponent
    rtsd    //Delayed return from subroutine - will
                //execute next three words
    move.w  #$7FFF,A0   //Max out mantissa
    nop     //Delay slot filler
    //end

NegO:
    move.w  #$007F,A     //Max out exponent
    rtsd    //Delayed return from subroutine - will
                //execute next three cycles
    move.w  #$8000,A0   //Most negative mantissa
    nop     //Delay slot filler
    //end

Underflow:
    cmp.w  #$FF80,Y0    //Check for underflow
    jge    Continue    //Not an error
    tst.w  A1           //Positive or negative underflow?
    jlt    NegU         //If negative, go to negative handler
    move.w #$FF80,A     //Minimum exponent
    rtsd
    move.w #$4000,A0   //Minimum normalized positive mantissa
    nop     //Filler for third delay slot
    //end

NegU:
    move.w  #$FF80,A     //Minimum exponent
    rtsd    //Delayed return from subroutine - will
                //execute next three words
    move.w  #$BFFF,A0   //Minimum (abs) normalized negative
                //mantissa
    nop     //filler for third delay slot
    //end of E_Err
}

```

7.23 FFabs

```

asm ffloat FFabs(register ffloat fnum)
{
    move.w  A1,Y0       //store fnum exp in Y0
    move.w  A0,A        //A holds mantissa of fnum
    abs     A           //full-width absolute value
    asr    A            //shift right to prevent overflow of clb
    jeq    Zero        //Don't normalize if zero

    //fnum != 0
    clb    A,X0        //Count sign bits
    asll.l X0,A        //Normalize

    sub     X0,Y0      //Adjust exponent
    inc.w  Y0         //Return to normal scale
}

```

```

        clb          Y0,X0          //check number of sign bits in exponent
        cmp.w       #8,X0          //If less than 8 (exp > 8 bits),
        jlt        Exp_Err        //jump to exponent exception handler

Continue:
        rtsd                //delayed return from subroutine
        move.w      A,A0          //Move mantissa of sum to lower word of ffnm1
                                   //(return value)
        move.w      Y0,A1          //Move exponent to upper word of ffnm1 (return
                                   //value)
        sxt.l A                //Sign-extend A to 36 bits
        //end of main abs function

Zero:
        rtsd                //Delayed return from subroutine - will execute
                                   //next three words
        move.w      #$FF80,A      //Set exp of sum to minimum
        clr.w A0              //Set mantissa of sum to 0
        //end of zero handler

Exp_Err:
        cmp.w      #$007F,Y0     //If not overflow, go to underflow check
        jle        Underflow     //Positive or negative overflow?
        tst.w      A1            //If negative, go to negative handler
        jlt        Neg0
        move.w      #$007F,A      //Max out exponent
        rtsd                //Delayed return from subroutine - will execute
                                   //next three words
        move.w      #$7FFF,A0     //Max out mantissa
        nop                //Delay slot filler
        //end

Neg0:
        move.w      #$007F,A      //Max out exponent
        rtsd                //Delayed return from subroutine - will execute
                                   //next three cycles
        move.w      #$8000,A0     //Most negative mantissa
        nop                //Delay slot filler
        //end

Underflow:
        cmp.w      #$FF80,Y0     //Check for underflow
        jge        Continue      //Not an error
        tst.w      A1            //Positive or negative underflow?
        jlt        NegU          //If negative, go to negative handler
        move.w      #$FF80,A      //Minimum exponent
        rtsd
        move.w      #$4000,A0     //Minimum normalized positive mantissa
        nop                //Filler for third delay slot
        //end

NegU:
        move.w      #$FF80,A      //Minimum exponent
        rtsd                //Delayed return from subroutine - will execute
                                   //next three words
        move.w      #$BFFF,A0     //Minimum (abs) normalized negative mantissa
        nop                //filler for third delay slot
        //end of E_Err
}

```


8 References

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<<http://www.ortodoxism.ro/datasheets2/d/0jayk8l9f7lua3gy5gyglyjs4x3y.pdf>>.

- [2] “DSP56800E Reference Manual.” 12 December 2006
<http://www.freescale.com/files/dsp/doc/ref_manual/DSP56800ERM.pdf>.

- [3] “Two’s Complement.” Wikipedia, the free encyclopedia. 5 December 2006
<http://en.wikipedia.org/wiki/Two%27s_complement>.