

MATH 293

PRELIM 1

SPRING 1990 # 5

3 a)

$$\begin{bmatrix} a & b \\ c & d \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} = \begin{bmatrix} 3x_1 \\ 2x_2 \end{bmatrix}$$

$$\begin{aligned} ax_1 + bx_2 &= 3x_1 &\Rightarrow b=0, ax_1 &= 3x_1 &\Rightarrow a=3 \\ cx_1 + dx_2 &= 2x_2 &\Rightarrow c=0, dx_2 &= 2x_2 &\Rightarrow d=2 \end{aligned}$$

$$A = \begin{bmatrix} 3 & 0 \\ 0 & 2 \end{bmatrix}$$

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PRELIM 2

SPRING 1992 #1

#6 a)

$$\begin{bmatrix} 1 & 2 & 3 \\ 3 & 1 & 2 \\ 2 & 3 & 1 \end{bmatrix} \begin{bmatrix} 5 \\ 7 \\ 9 \end{bmatrix} = \begin{bmatrix} 5+14+27 \\ 15+7+18 \\ 10+21+9 \end{bmatrix} = \begin{bmatrix} 46 \\ 30 \\ 40 \end{bmatrix}$$

$$b) \begin{bmatrix} 0 & 1 \\ 2 & 0 \end{bmatrix} \begin{bmatrix} 5 & 7 \\ 9 & 11 \end{bmatrix} = \begin{bmatrix} 0+9 & 0+11 \\ 10+0 & 14+0 \end{bmatrix} = \begin{bmatrix} 9 & 11 \\ 10 & 14 \end{bmatrix}$$

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P(7/21)

SUMMER 1992 #1

#7

$$a) AB = \begin{bmatrix} -1 & 2 & 3 \\ 4 & 1 & -5 \end{bmatrix} \begin{bmatrix} 1 & 2 \\ 0 & -1 \\ 1 & 1 \end{bmatrix} = \begin{bmatrix} -1+0+3 & -2-2+3 \\ 4+0-5 & 2-1-5 \end{bmatrix} = \begin{bmatrix} 2 & -1 \\ -1 & 2 \end{bmatrix}$$

$$b) BA = \begin{bmatrix} 1 & 2 \\ 0 & -1 \\ 1 & 1 \end{bmatrix} \begin{bmatrix} -1 & 2 & 3 \\ 4 & 1 & -5 \end{bmatrix} = \begin{bmatrix} -1+8 & 2+2 & 3-10 \\ 0-4 & 0-1 & 0+5 \\ -1+4 & 2+1 & 3-5 \end{bmatrix} = \begin{bmatrix} -7 & 4 & -7 \\ -4 & -1 & 5 \\ 3 & 3 & -2 \end{bmatrix}$$

$$c) A(BC) = \begin{bmatrix} -1 & 2 & 3 \\ 4 & 1 & -5 \end{bmatrix} \begin{bmatrix} 1 & 2 \\ 0 & -1 \\ 1 & 1 \end{bmatrix} \begin{bmatrix} -1 & 1 & 0 & -3 & 2 \\ 0 & 2 & 1 & -1 & 1 \end{bmatrix}$$

$$= \begin{bmatrix} -1 & 2 & 3 \\ 4 & 1 & -5 \end{bmatrix} \begin{bmatrix} -1 & 5 & 2 & -5 & 4 \\ 0 & -2 & -1 & 1 & -1 \\ -1 & 3 & 1 & -4 & 3 \end{bmatrix} = \begin{bmatrix} -2 & 0 & 2 & -5 & 3 \\ 1 & 3 & 2 & 1 & 0 \end{bmatrix}$$

$$d) CB = \begin{bmatrix} -1 & 1 & 0 & -3 & 2 \\ 0 & 2 & 1 & -1 & 1 \end{bmatrix} \begin{bmatrix} 1 & 2 \\ 0 & -1 \\ 1 & 1 \end{bmatrix} \quad \underline{\text{DNE}}$$

14) FALSE, ORDER MATTERS IN MATRIX MULTIPLICATION

$$(A+B)(A+B) = A^2 + AB + BA + B^2$$

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FINAL

SPRING 1996 #35

16) TRUE.

$$(A^T B^T)^T = (B^T)^T (A^T)^T = BA \quad (\text{THEOREM 3 p. 106})$$

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FALL 1997 #1

#16. a)

$$\begin{aligned} & \left[\begin{array}{cccc|c} 0 & 1 & 1 & -1 & 1 \\ 1 & -1 & 0 & 2 & 3 \\ -1 & 2 & 1 & -3 & -2 \end{array} \right] \xrightarrow{\text{SWAP ROW 1, ROW 2}} \left[\begin{array}{cccc|c} 1 & -1 & 0 & 2 & 3 \\ 0 & 1 & 1 & -1 & 1 \\ -1 & 2 & 1 & -3 & -2 \end{array} \right] \xrightarrow{\text{ROW 3} + \text{ROW 1}} \left[\begin{array}{cccc|c} 1 & -1 & 0 & 2 & 3 \\ 0 & 1 & 1 & -1 & 1 \\ 0 & 1 & 1 & -1 & 1 \end{array} \right] \\ & \xrightarrow{\text{ROW 3} - \text{ROW 2}} \left[\begin{array}{cccc|c} 1 & -1 & 0 & 2 & 3 \\ 0 & 1 & 1 & -1 & 1 \\ 0 & 0 & 0 & 0 & 0 \end{array} \right] \xrightarrow{\text{ROW 1} + \text{ROW 2}} \left[\begin{array}{cccc|c} 1 & 0 & 1 & 1 & 4 \\ 0 & 1 & 1 & -1 & 1 \\ 0 & 0 & 0 & 0 & 0 \end{array} \right] \end{aligned}$$

$$\Rightarrow \begin{aligned} x_1 + y_3 + x_4 &= 4 & x_1 &= 4 - x_3 - x_4 \\ x_2 + y_3 - x_4 &= 1 & x_2 &= 1 - x_3 + x_4 \\ y_3 &= \text{free} & x_3 &= x_3 \\ x_4 &= \text{free} & x_4 &= x_4 \end{aligned}$$

$$\underline{\underline{\underline{x} = \begin{bmatrix} 4 \\ 1 \\ 0 \\ 0 \end{bmatrix} + x_3 \begin{bmatrix} -1 \\ -1 \\ 1 \\ 0 \end{bmatrix} + x_4 \begin{bmatrix} -1 \\ 1 \\ 0 \\ 1 \end{bmatrix}}}$$

b)

$$\begin{bmatrix} 1 & A \\ -1 & C \end{bmatrix} \begin{bmatrix} 1 & A \\ -1 & C \end{bmatrix} = 0$$

$$\begin{bmatrix} 1-A & A+AC \\ -1-C & -A+C^2 \end{bmatrix} \Rightarrow \begin{aligned} 1-A &= 0 & -1-C &= 0 & A(1+C) &= 0 & -A+C^2 &= 0 \\ A &= 1 & C &= -1 & A(1-1) &= 0 & -(1)+(-1)^2 &= 0 \\ & & & & 0 &= 0 & 0 &= 0 \end{aligned}$$

$$\underline{\underline{\underline{B = \begin{bmatrix} 1 & 1 \\ -1 & -1 \end{bmatrix}}}}}$$