

# Particle Dynamics

Error in ODE solution (soln)



Back to particle dynamics

General Problem:  $\vec{F} = \vec{F}(\vec{r}, \vec{v}, t)$

Example: gravity  $\vec{F} = \begin{bmatrix} -mg\hat{j} \\ -\frac{MmG}{r^2}\hat{r} \end{bmatrix}$  near earth  
big G

spring:  $\vec{F} = K(|\vec{r}| - l_0) \frac{\vec{r}}{|\vec{r}|}$

drag:  $\vec{F} = \begin{bmatrix} -c\vec{v} \\ -c|\vec{v}|\vec{v} \end{bmatrix}$  linear viscous  
quadratic drag

You know the particles mass, position, velocity, time  $K \rightarrow \vec{F}(\vec{r}, \vec{v}, t)$

$$\vec{F} = m\vec{a} \quad \vec{a} = \frac{\vec{F}}{m}$$

$$\dot{\vec{r}} = \vec{v}$$
$$\dot{\vec{v}} = \vec{a} = \frac{\vec{F}}{m}$$

$$\dot{z} = f(z, t) \quad z = \begin{bmatrix} z_1 \\ z_2 \\ z_3 \dots \end{bmatrix} = \begin{bmatrix} r_x \\ r_y \\ v_x \\ v_y \end{bmatrix}$$

## Ballistics Problem

$$\vec{F} = -c|\vec{v}|\vec{v} + -mg\hat{s} \quad C = C_0 * \rho_{air} * A_{cross}(ball)$$

$$\begin{aligned} \text{LMB: } \vec{F} &= m\vec{a} \\ &= -c|\vec{v}|\vec{v} - mg\hat{s} = m\vec{a} \\ &= -\frac{c}{m}|\vec{v}|\vec{v} - g\hat{s} = \vec{a} \end{aligned}$$

$$\begin{aligned} \dot{\vec{r}} &= \vec{v} \\ \dot{\vec{v}} &= \vec{a} = -\frac{c}{m}|\vec{v}|\vec{v} - g\hat{s} \end{aligned} \quad \left. \vphantom{\begin{aligned} \dot{\vec{r}} &= \vec{v} \\ \dot{\vec{v}} &= \vec{a} = -\frac{c}{m}|\vec{v}|\vec{v} - g\hat{s} \end{aligned}} \right\} 4 \text{ ODE's}$$

$$\begin{aligned} \Delta r &\approx \dot{\vec{r}} \Delta t \\ \Delta v &\approx \dot{\vec{v}} \Delta t \end{aligned} \quad \left. \vphantom{\begin{aligned} \Delta r &\approx \dot{\vec{r}} \Delta t \\ \Delta v &\approx \dot{\vec{v}} \Delta t \end{aligned}} \right\} \text{Euler's method}$$

Set this up in the computer